



**COMPUTER SOCIETY OF INDIA (CSI)
COEP TECH STUDENT CHAPTER**



PRESENTS

**CODE
QUEST
5.0**

EDITORIAL

KUNAL'S DILEMMA

EXPLANATION

The problem requires Kunal to allocate his available time fractionally across multiple slots to meet the required work quotas for both ASCII and CSI on a given day. The goal is to determine whether he can successfully distribute his time to satisfy the daily requirements.

1. Sorting Slots by Efficiency:

- Each time slot has two productivity values: (A_i) (ASCII work) and (C_i) (CSI work).
- To optimize time allocation, we compute the efficiency ratio (A_i/C_i) (if ($C_i \neq 0$), otherwise consider it as infinitely large).
- We then sort the slots in descending order of this efficiency ratio, prioritizing slots where ASCII work is more efficient.

EXPLANATION

2. Prefix Sums for Efficient Lookups:

- We maintain a prefix sum array ($C[]$), where ($C[i]$) stores the cumulative ASCII work if all time from the first (i) slots is dedicated to ASCII.

- We also maintain a suffix sum array ($E[]$), where ($E[i]$) stores the cumulative CSI work if all remaining time from slot (i) onward is dedicated to CSI.

3. Checking Daily Requirements Efficiently:

- For each day, given required ASCII work (A_{total}) and CSI work (C_{total}):

- We find the smallest prefix index (i) where ($C[i] \geq A_{total}$). This tells us how many slots are needed to satisfy the ASCII work requirement.

EXPLANATION

- We then compute how much time fractionally remains for CSI work.

- If the total achievable CSI work (from partial and remaining slots) is enough, the answer for that day is 'P' (Possible), otherwise 'N' (Not possible).

4. Efficiency Considerations:

- Sorting the slots takes ($O(S \log S)$).
- Building prefix and suffix sums takes ($O(S)$).
- Checking for each day's requirement is done in ($O(\log S)$) using binary search.
- This ensures the approach efficiently handles large constraints.

EXAMPLE

Input:

1

1 3

3 2

4 1

2 3

5 5

Explanation of input:

- 1 test case
- 1 day and 3 slots
- Slots:
 - Slot 1: (3 ASCII, 2 CSI)
 - Slot 2: (4 ASCII, 1 CSI)
 - Slot 3: (2 ASCII, 3 CSI)
- Required work on Day 1: 5 ASCII, 5 CSI

EXAMPLE

Step 1: Compute Efficiency and Sort

- Compute efficiency ratios:
 - Slot 1: ($3/2 = 1.5$)
 - Slot 2: ($4/1 = 4.0$) (Highest, prioritize ASCII)
 - Slot 3: ($2/3$ approx 0.67) (Least efficient for ASCII)
- Sort in decreasing order:
 - Slot 2: (4 ASCII, 1 CSI)
 - Slot 1: (3 ASCII, 2 CSI)
 - Slot 3: (2 ASCII, 3 CSI)

Step 2: Compute Prefix and Suffix Arrays

- Prefix sum for ASCII:
 - $C[0] = 4$
 - $C[1] = 4 + 3 = 7$
 - $C[2] = 7 + 2 = 9$
- Suffix sum for CSI:
 - $E[2] = 3$
 - $E[1] = 2 + 3 = 5$
 - $E[0] = 1 + 5 = 6$

EXAMPLE

Step 3: Check Requirements

- Need 5 ASCI and 5 CSI
- Find ASCI requirement:
 - ($C[0] = 4$) (insufficient)
 - ($C[1] = 7$) (sufficient, so need up to slot 1)
- Compute fractional usage:
 - Need extra 1 ASCI from slot 2.
 - Slot 2: ($1/3$) of time spent on ASCI Leaves ($2/3$) for CSI.
 - ($2/3$ times 2 = 1.33) CSI from slot 2.
 - Total CSI: ($1.33 + 5 = 6.33$) (Enough!)
- Result: 'P'

Final Output:

P

SOLUTION

```
1 import bisect
2 def solve():
3     # Read number of days and slots
4     num_days, num_slots = [int(_) for _ in input().split()]
5     daily_requirements = []
6     slots = []
7     # Read slot values
8     for _ in range(num_slots):
9         slots.append([int(_) for _ in input().split()])
10    # Read daily requirements
11    for _ in range(num_days):
12        daily_requirements.append([int(_) for _ in input().split()])
13    # Sort slots based on efficiency (ASCII work per unit CSI work)
14    slots.sort(key=lambda x: float(x[0]) / x[1] if x[1] else 100000)
15    # Compute prefix sum for ASCII work
16    ascii_prefix_sum = []
17    total_ascii = 0
18    for slot in slots:
19        total_ascii += slot[1]
20        ascii_prefix_sum.append(total_ascii)
21    # Compute suffix sum for CSI work
22    csi_suffix_sum = []
23    total_csi = 0
24    for slot in reversed(slots):
25        total_csi += slot[0]
26        csi_suffix_sum.append(total_csi)
27    csi_suffix_sum = csi_suffix_sum[::-1]
28    result_string = ""
29    # Process each day's requirements
30    for required_csi, required_ascii in daily_requirements:
31        slot_index = bisect.bisect_left(ascii_prefix_sum, required_ascii) # Find minimum slot index to meet ASCII requirement
32        if slot_index == num_slots: # If requirement can't be met, add 'N'
33            result_string += "N"
34            continue
35        remaining_ascii = ascii_prefix_sum[slot_index] - required_ascii # Remaining ASCII work
36        # Convert excess ASCII work to CSI work
37        converted_csi = float(remaining_ascii * slots[slot_index][0]) / slots[slot_index][1] if slots[slot_index][1] else slots[slot_index][0]
38        # Total possible CSI work
39        total_possible_csi = converted_csi + csi_suffix_sum[slot_index+1] if slot_index+1 < num_slots else converted_csi
40        if total_possible_csi >= required_csi: # Check if CSI requirement is met
41            result_string += "P"
42        else:
43            result_string += "N"
44
45    return result_string
46
47 num_test_cases = int(input())
48 for _ in range(num_test_cases):
49     result = solve()
50     print(result)
51
```